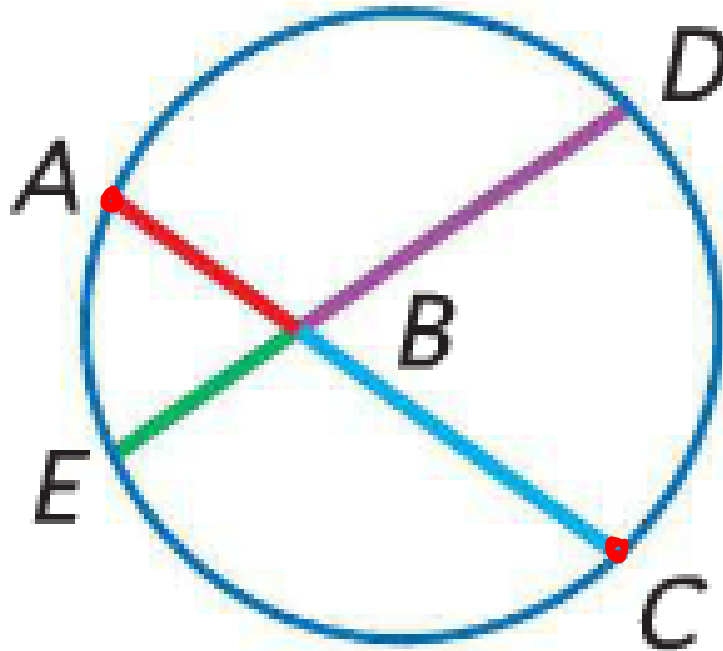


Special Segments in a Circle

Segments of Chords Theorem

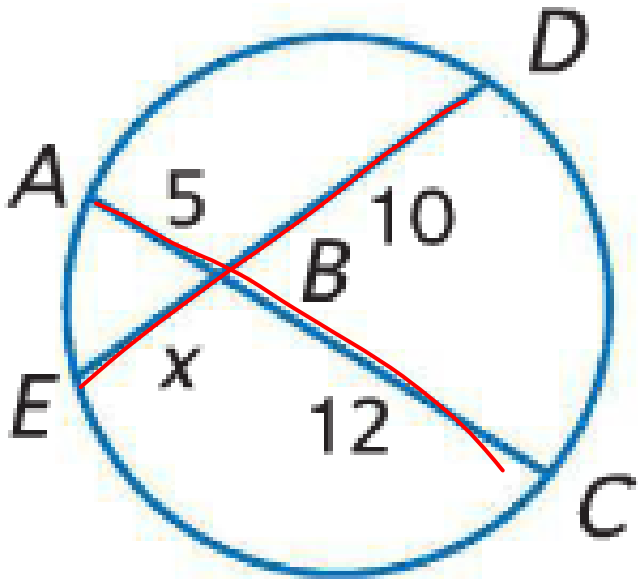
X

- If two chords intersect in a circle, then the products of the lengths of the chord segments are equal.



Examples

- Find x.



$$5 \cdot 12 = 10 \cdot x$$

$$\frac{60}{10} = \frac{10x}{10}$$

$$6 = x$$

Examples

- Find x .

- $5 * 12 = x * 10$

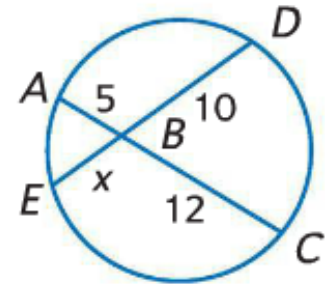
The products of the lengths of the chord segments are equal.

- $60 = 10x$

Multiply

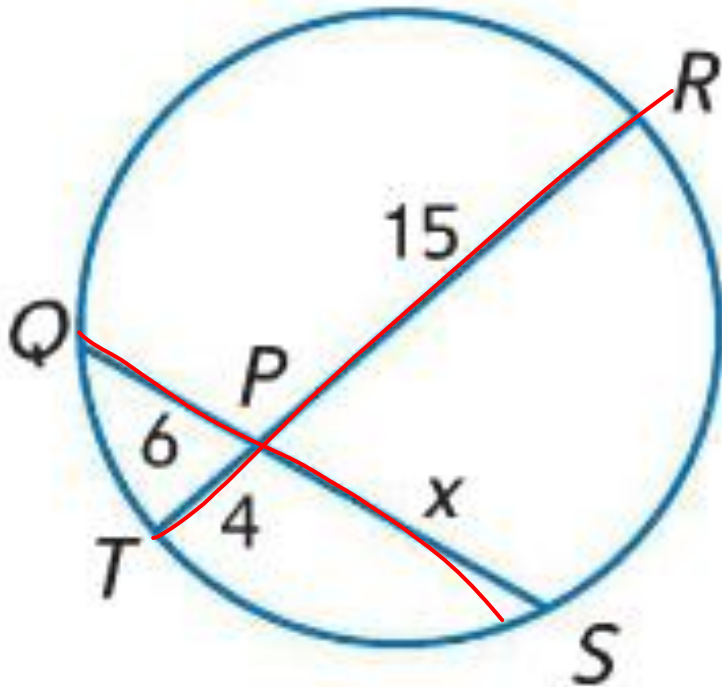
- $6 = x$

Divide both sides by 10



Examples

- Find x.



$$4 \cdot 15 = 6 \cdot x$$

$$\frac{15}{10}$$

$$\frac{60}{6} = \frac{6x}{6}$$

$$10 = x$$

Examples

- Find x .

- $4 * 15 = 6 * x$

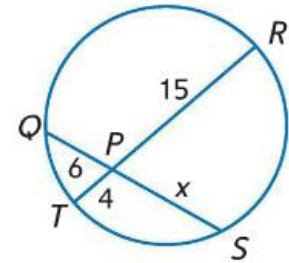
The products of the lengths of the chord segments are equal.

- $60 = 6x$

Multiply

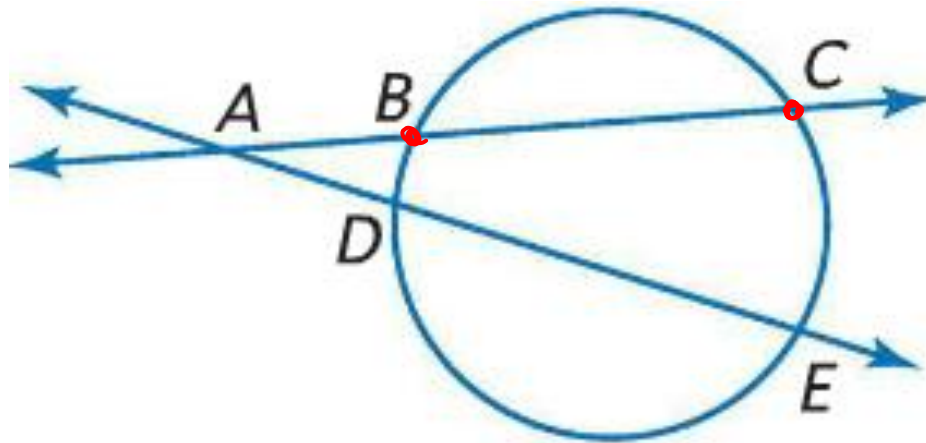
- $10 = x$

Divide both sides by 6



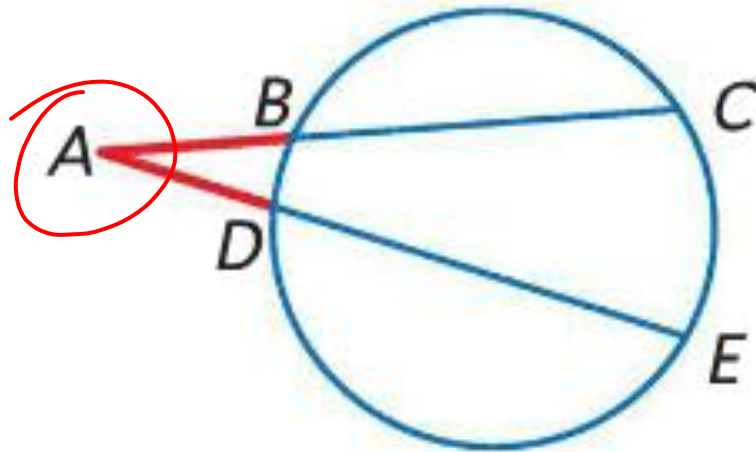
Secant Segments

- A secant segment is a segment of a secant line that has exactly one endpoint on the circle.
- A secant segment that lies in the exterior of the circle is called an external secant segment.



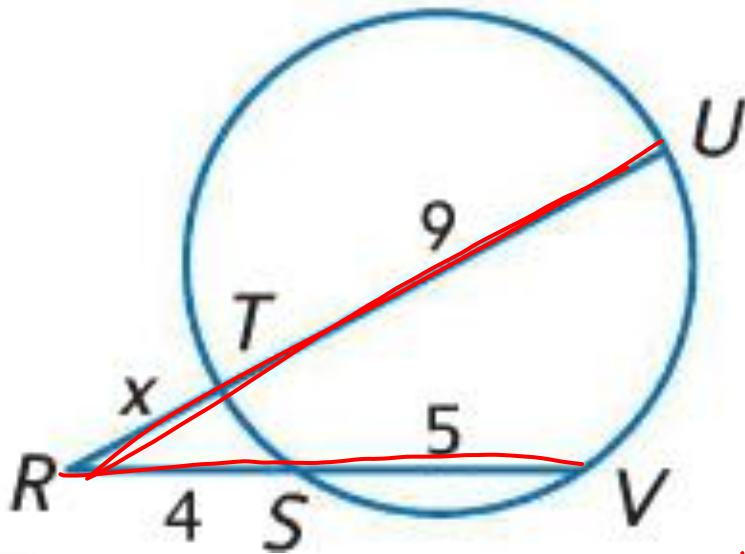
Secant Segments Theorem

- If two secants intersect in the exterior of a circle, then the product of the measures of one secant segment and its external secant is equal to the product of the measures of the other secant and its external secant segment.



Examples

- Find x.



$$(4+5)4 = (9+x)x$$

$$36 = x^2 + 9x$$

$$-36 \quad -36$$

$$0 = x^2 + 9x - 36$$

$$0 = (x-3)(x+12)$$

$$\begin{array}{r} -36 \\ \hline +36 \\ \hline -18 \\ \hline -3 +12 \\ \hline 4 \quad 9 \\ 6 \quad 6 \end{array}$$

$$\boxed{x=3} \times 2$$

Examples

- Find x .

- $(9 + x) * x = 9 * 4$

- $9x + x^2 = 36$

- $x^2 + 9x - 36 = 0$

- $(x + 12)(x - 3) = 0$

- $x = \cancel{-12}, 3; x = 3$

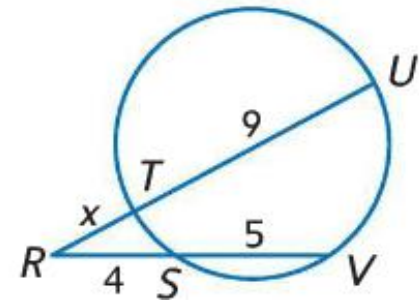
Whole line times outside piece on both sides

Multiply

Set equation equal to zero

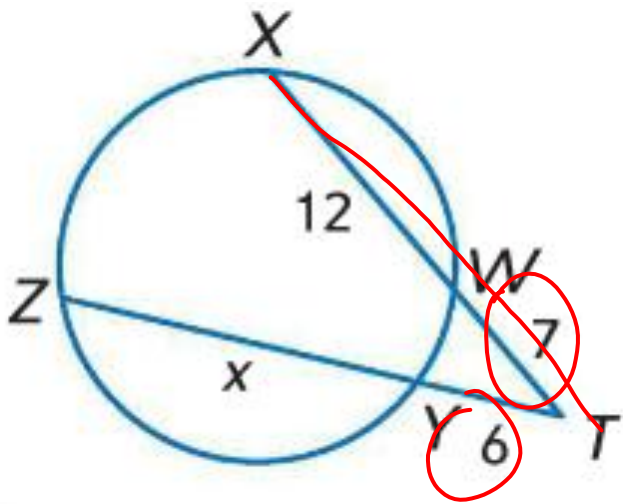
Factor the equation

Choose sensible answer



Examples

- Find x.



$$19.7 = (x+6)6$$

$$133 = 6x + 36$$
$$-36 \quad -36$$

$$\frac{97}{6} = \frac{6x}{6}$$

$$16.17 = x$$

Examples

- Find x .

- $(x + 6) * 6 = 19 * 7$

Whole line times outside piece on both sides

- $6x + 36 = 133$

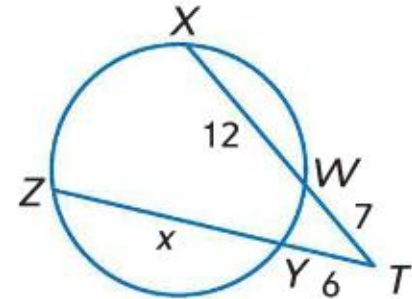
Multiply

- $6x = 97$

Subtract 36 from both sides

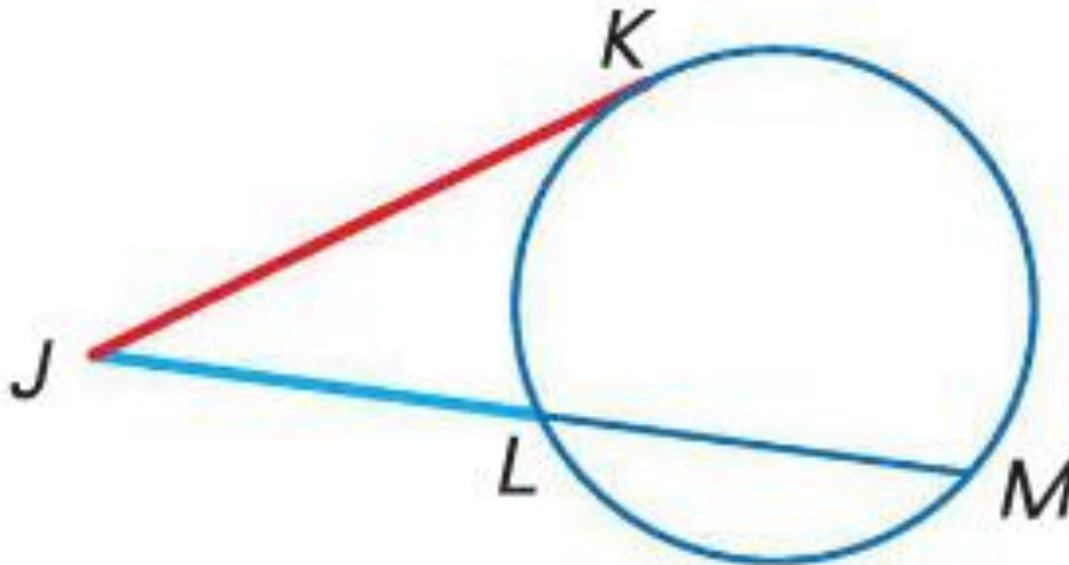
- $x = 16.17$

Divide both sides by 6



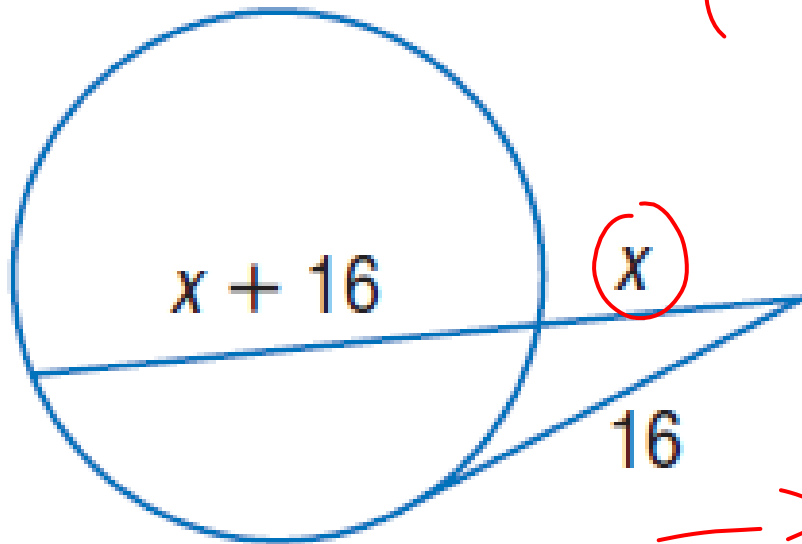
Tangent-Secant Segment Theorem

- If a tangent and a secant intersect in the exterior of a circle, then the square of the measure of the tangent is equal to the product of the measures of the secant and its external secant segment.



Examples

- Find x . Assume that segments that appear to be tangent are tangent.



$$(x + 16 + x)x = 16^2$$

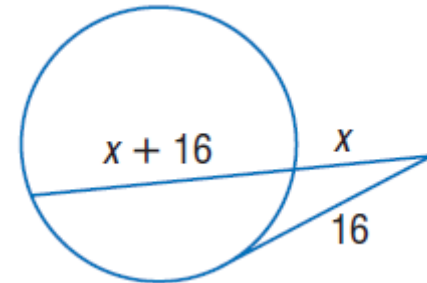
$$2x^2 + 16x = 256$$

$$\frac{2x^2 + 16x - 256 = 0}{2}$$

$$\rightarrow x^2 + 8x - 128 = 0 \leftarrow$$

Examples

- Find x . Assume that segments that appear to be tangent are tangent.



- $16^2 = x(x + x + 16)$ Tangent-Secant Segment Theorem
- $256 = 2x^2 + 16x$ Simplify the equation
- $0 = 2x^2 + 16x - 256$ Subtract 256 from both sides
- $0 = x^2 + 8x - 128$ Reduce the equation
- $0 = (x + 16)(x - 8)$ Factor the equation
- $x = -16, 8$ Solve;
- $x = 8$ Choose sensible answer