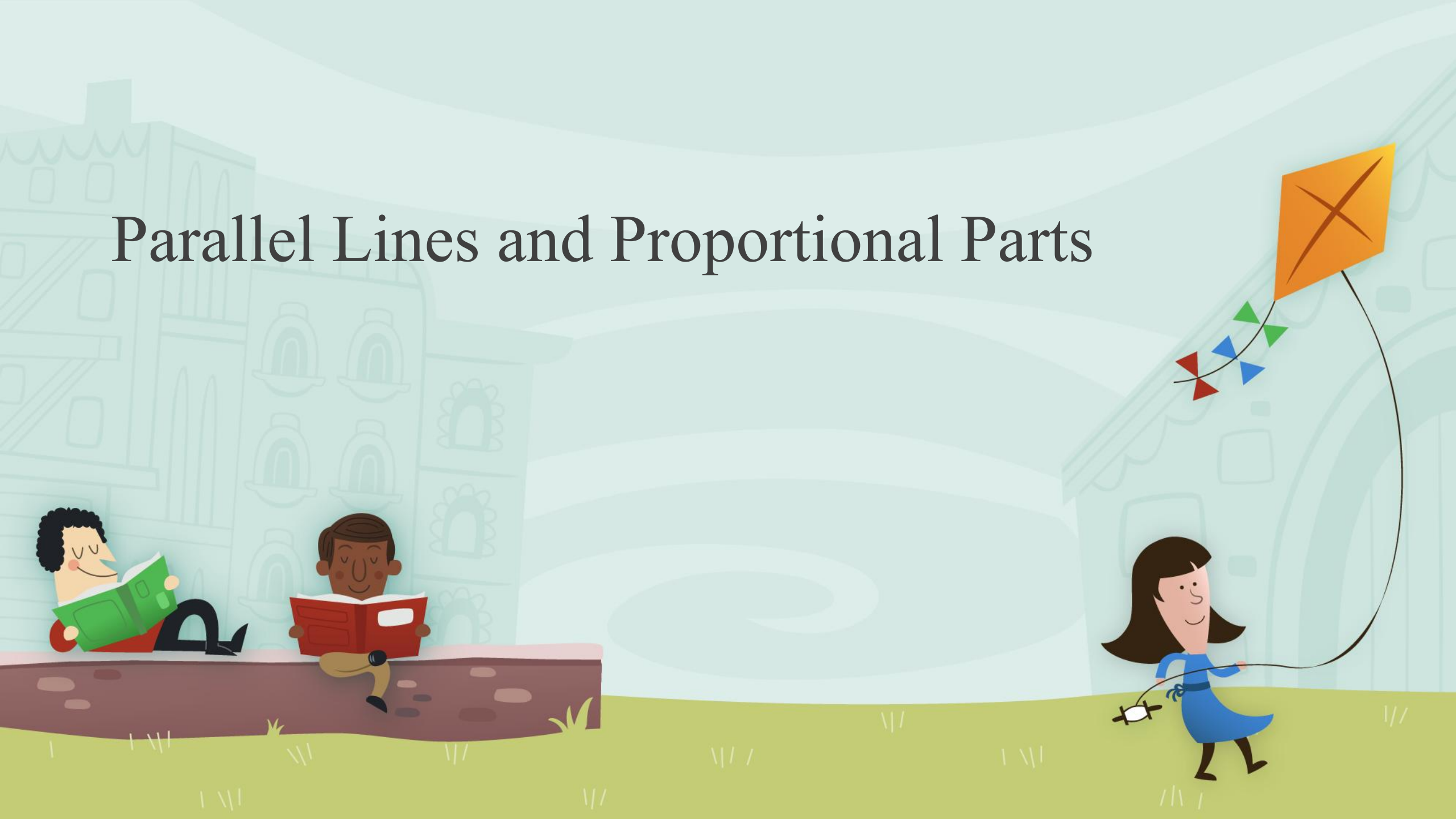
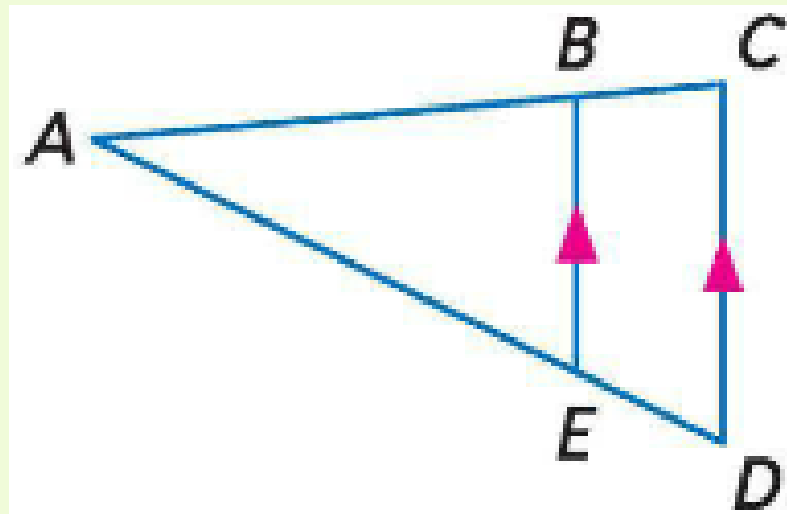


Parallel Lines and Proportional Parts



Triangle Proportionality Theorem

- If a line is parallel to one side of a triangle and intersects the other two sides, then it divides the sides into segments of proportional lengths.

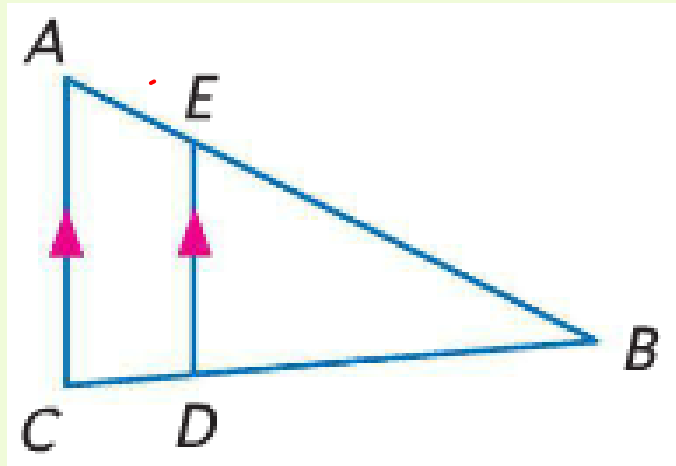


$$\text{If } \overline{BE} \parallel \overline{CD}, \text{ then } \frac{AB}{BC} = \frac{AE}{ED}.$$



Converse of Triangle Proportionality Theorem

- If a line intersects two sides of a triangle and separates the sides into proportional corresponding segments, then the line is parallel to the third side of the triangle.

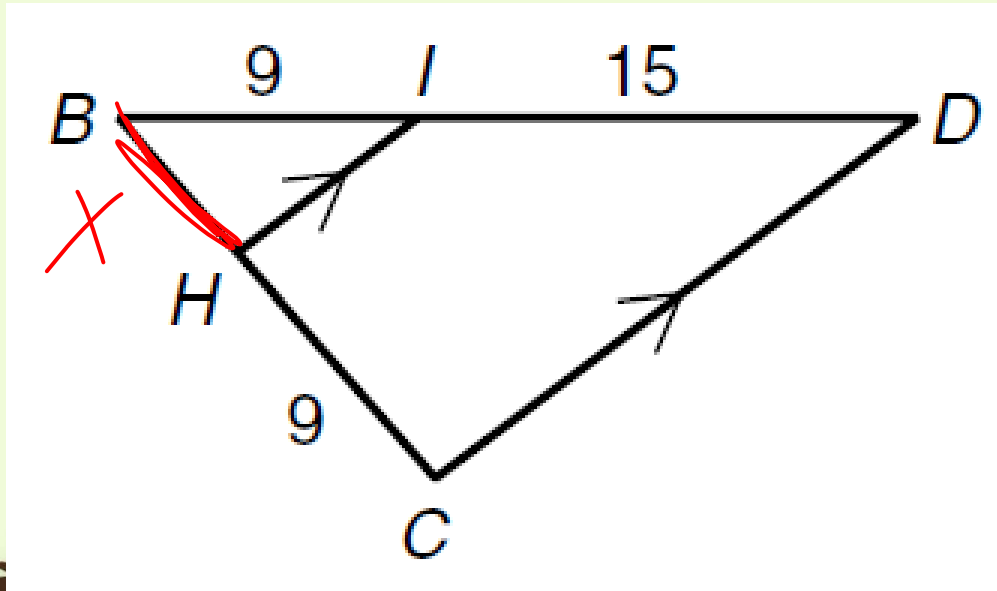


$$\text{If } \frac{AE}{EB} = \frac{CD}{DB}, \text{ then } \overline{AC} \parallel \overline{ED}.$$



Examples

- Find the length of BH.



$$\frac{x}{9} \times \frac{9}{15}$$

$$\frac{9}{15} \times \frac{x}{9}$$

$$\frac{81}{15} = \frac{15x}{15}$$

$$5.4 = x$$

$$\frac{9}{9} \rightarrow 3$$

$$\frac{15}{15} \rightarrow 5$$

$$\frac{3}{5} \times \frac{x}{9}$$

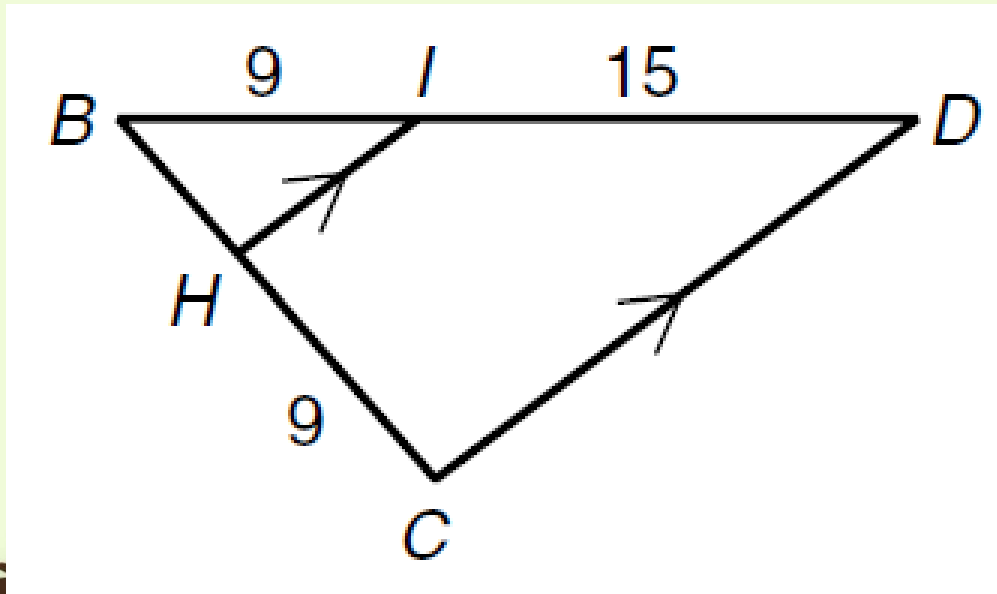
$$\frac{27}{5} = \frac{5x}{5}$$

$$5.4 = x$$



Examples

- Find the length of BH.



$$\frac{x}{9} = \frac{9}{15}$$

$$15x = 81$$

$$x = \frac{81}{15}$$

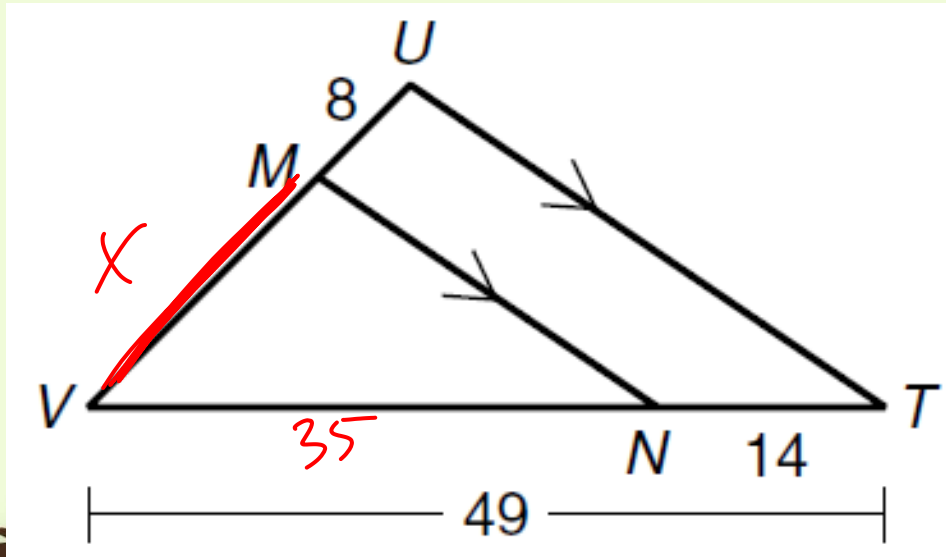
$$x = 5.4$$



$$MV = 28$$

Examples

- Find the length of MV.



$$\frac{X}{35} = \frac{8}{14} \cdot \frac{4}{7}$$

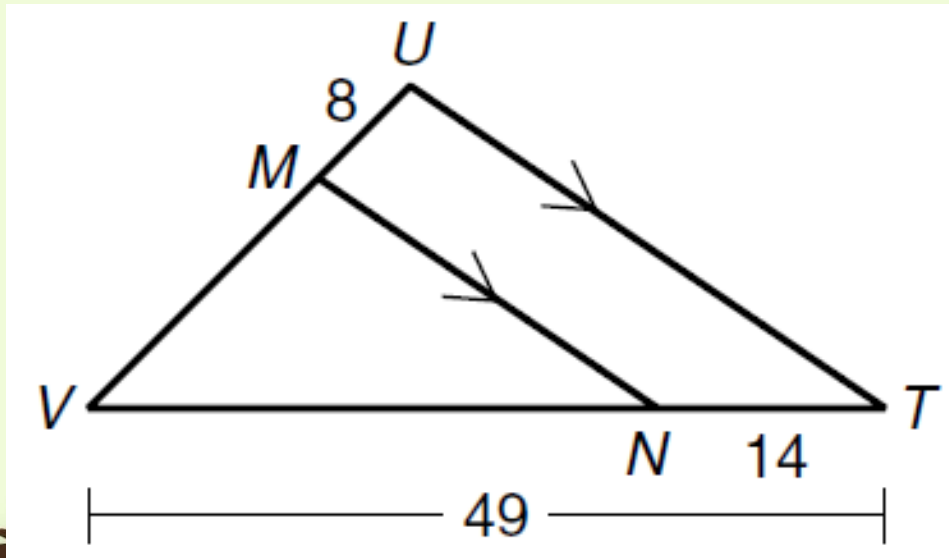
$$\sqrt{X} = \frac{140}{7}$$

$$X = 20$$



Examples

- Find the length of MV.



$$\frac{x}{8} = \frac{35}{14}$$

$$14x = 280$$

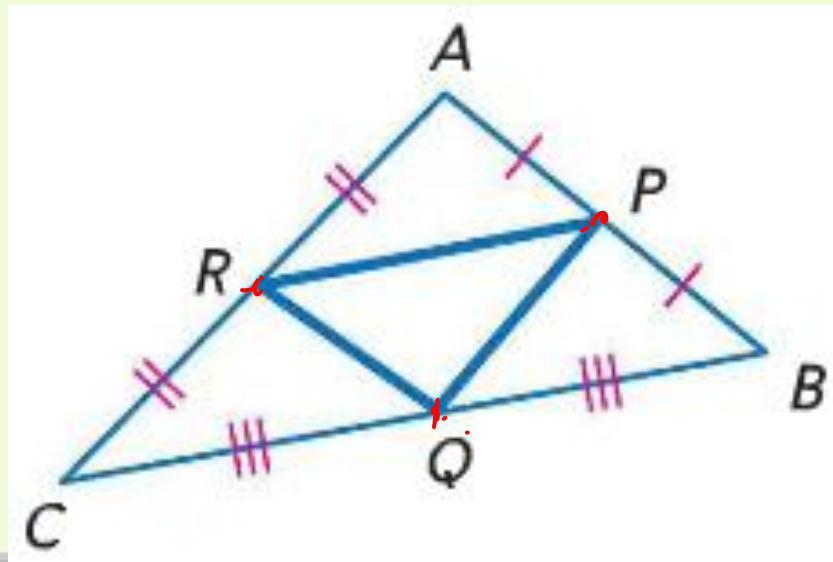
$$x = \frac{280}{14}$$

$$x = 20$$



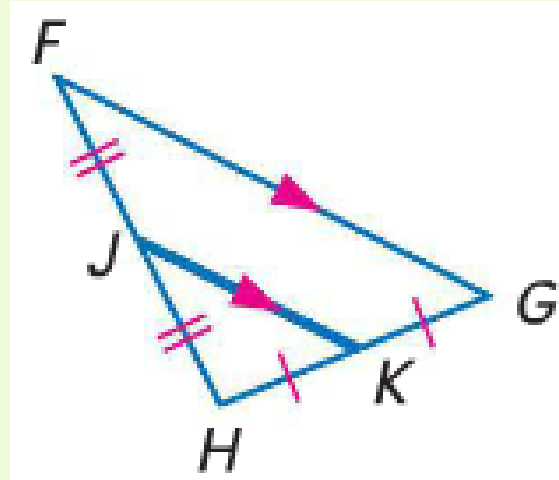
Midsegment

- A midsegment of a triangle is a segment with endpoints that are the midpoints of two sides of the triangle.
- Every triangle has three midsegments.



Triangle Midsegment Theorem

- A midsegment of a triangle is parallel to one side of the triangle, and its length is one half the length of that side.

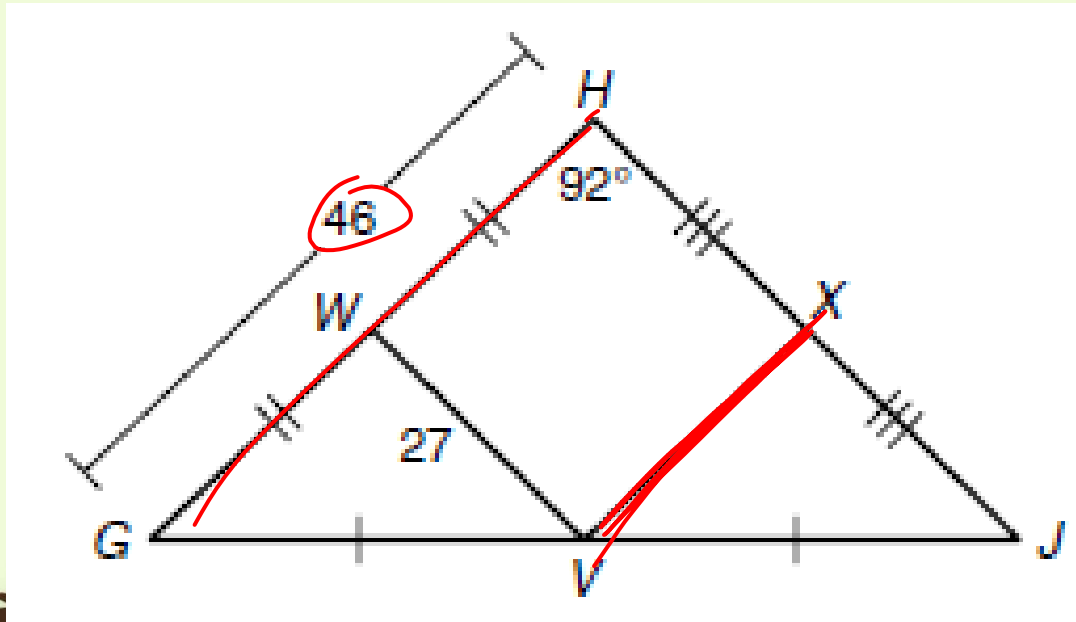


If J and K are midpoints of \overline{FH} and \overline{HG} , respectively, then $\overline{JK} \parallel \overline{FG}$ and $JK = \frac{1}{2}FG$.



Examples

- Find the measure of VX .



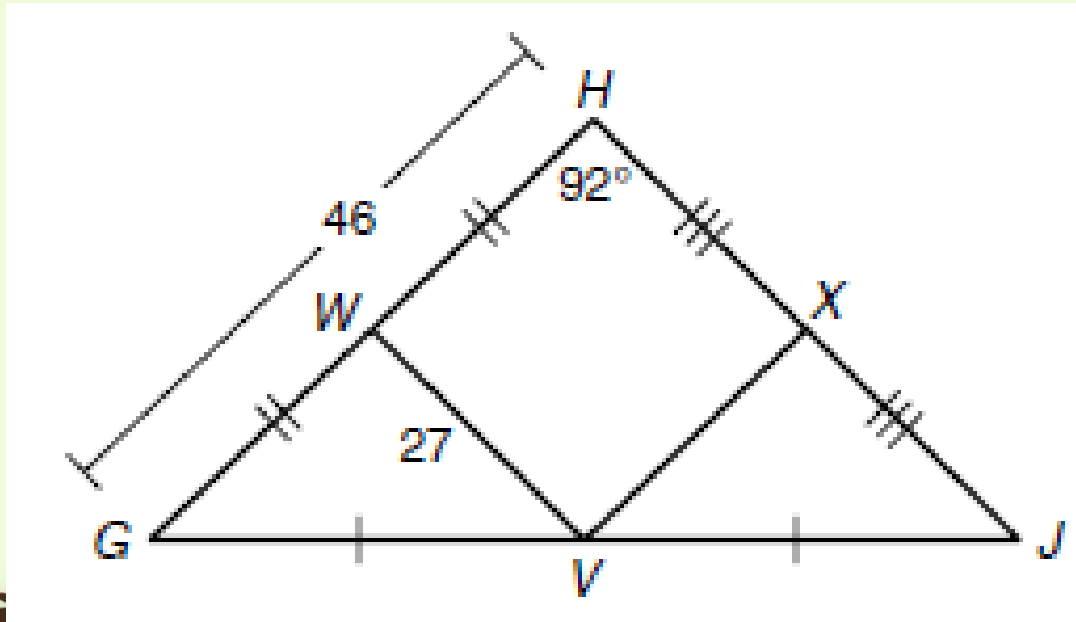
$$VX = 27$$

23
19
54



Examples

- Find the measure of VX.



$$VX = \frac{1}{2}GH$$

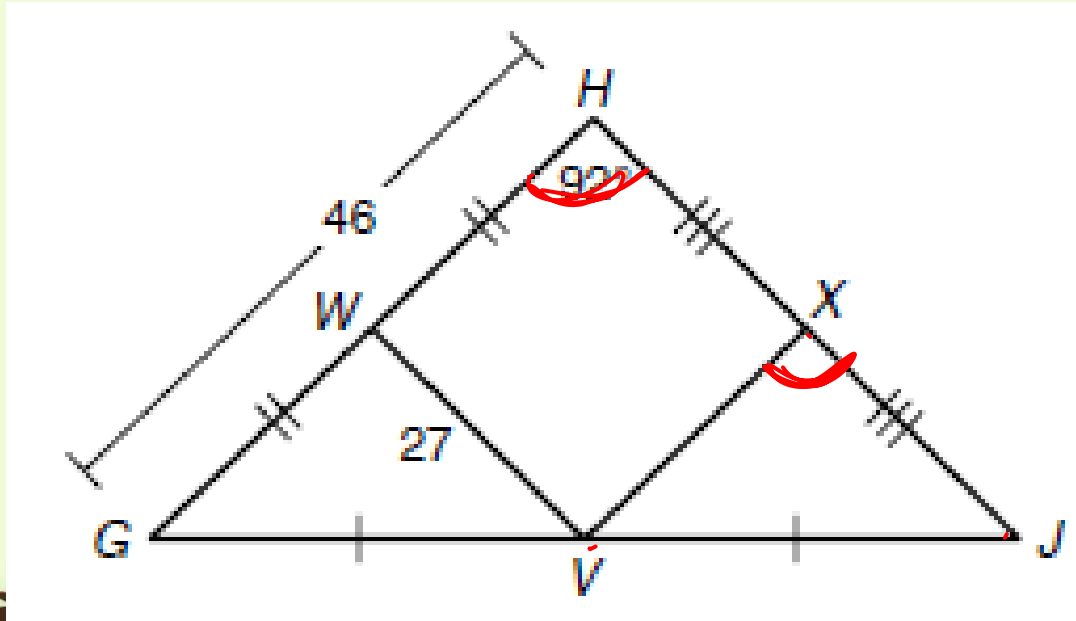
$$VX = \frac{1}{2}(46)$$

$$VX = 23$$



Examples

- Find the measure of $m\angle VXJ$.



$$\angle VXJ = 46$$

$$88$$

$$81$$

$$92$$

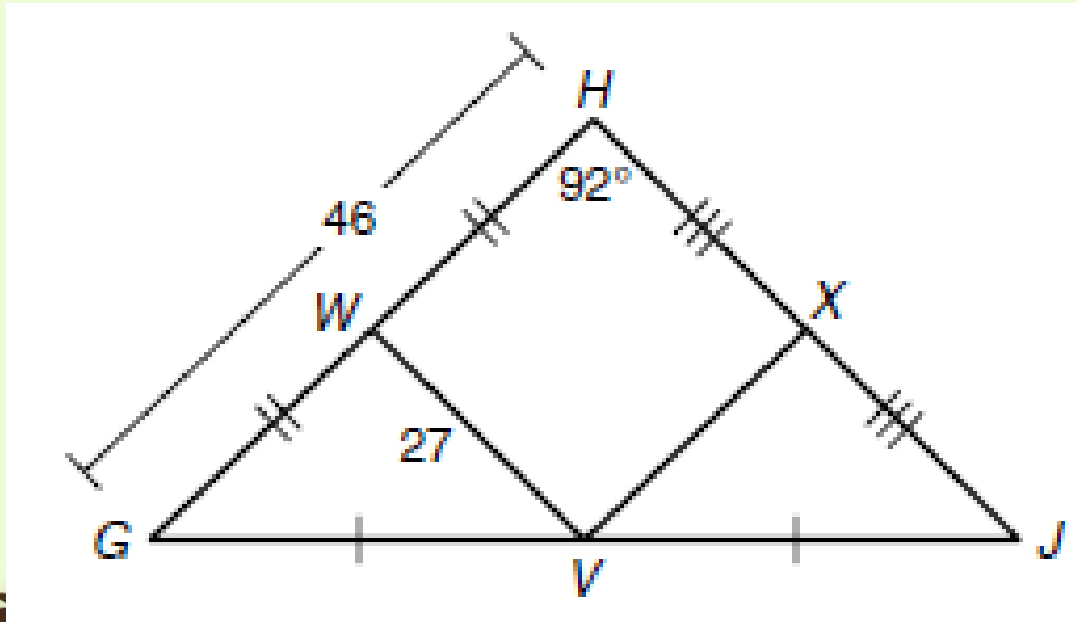
$$96$$

$$69$$



Examples

- Find the measure of $m\angle VXJ$.

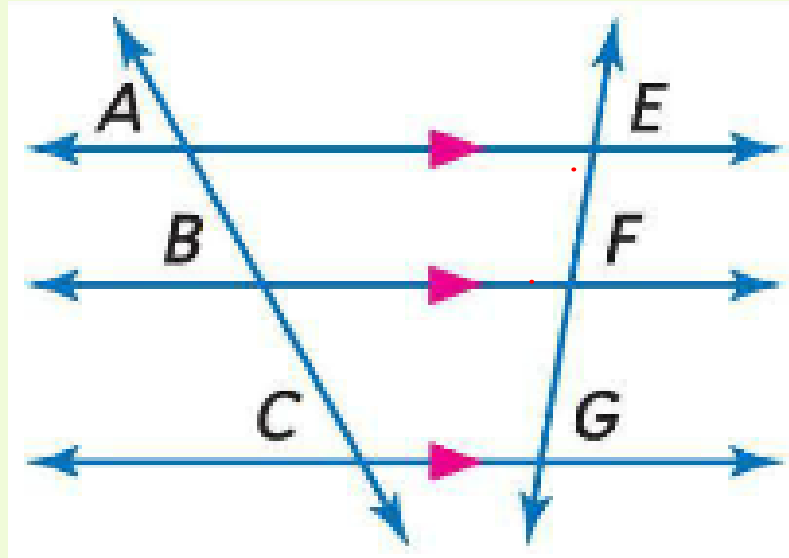


Since midsegments are parallel to the sides of the triangle, then $m\angle VXJ$ has to be equal to $m\angle WHX$ since they are corresponding angles.



Proportional Parts of Parallel Lines

- If three or more parallel lines intersect two transversals, then they cut off the transversals proportionally.

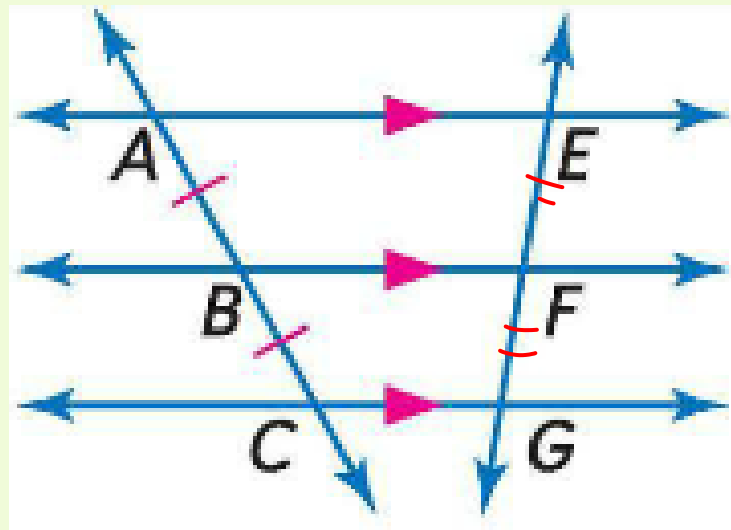


$$\text{If } \overline{AE} \parallel \overline{BF} \parallel \overline{CG}, \text{ then } \frac{AB}{BC} = \frac{EF}{FG}$$



Congruent Parts of Parallel Lines

- If three or more parallel lines cut off congruent segments on one transversal, then they cut off congruent segments on every transversal.

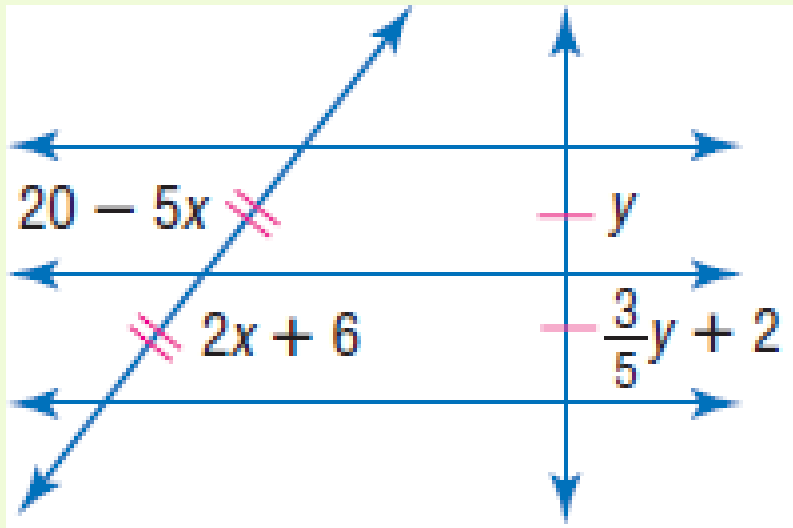


If $\overline{AE} \parallel \overline{BF} \parallel \overline{CG}$, and $\overline{AB} \cong \overline{BC}$,
then $\overline{EF} \cong \overline{FG}$.



Examples

- Find x and y.

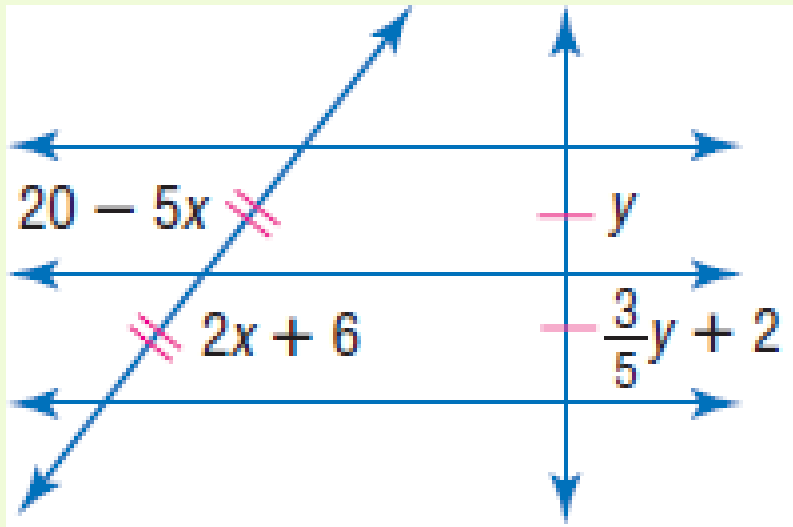


$$20 - 5x = 2x + 6$$
$$-6 + 5x + 5x = 2x + 6 - 6$$
$$14 = 7x$$
$$\frac{14}{7} = \frac{7x}{7}$$
$$2 = x$$
$$5 \left[y = \frac{3}{5}y + 2 \right]$$
$$5y = 3y + 10$$
$$-3y + 3y = 3y + 10 - 3y$$
$$2y = 10$$
$$\frac{2y}{2} = \frac{10}{2}$$
$$y = 5$$



Examples

- Find x and y .



Since the segments are congruent, simply set them equal to each other.

$$20 - 5x = 2x + 6$$

$$14 = 7x$$

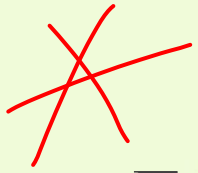
$$2 = x$$

$$y = \frac{3}{5}y + 2$$

$$\frac{2}{5}y = 2$$

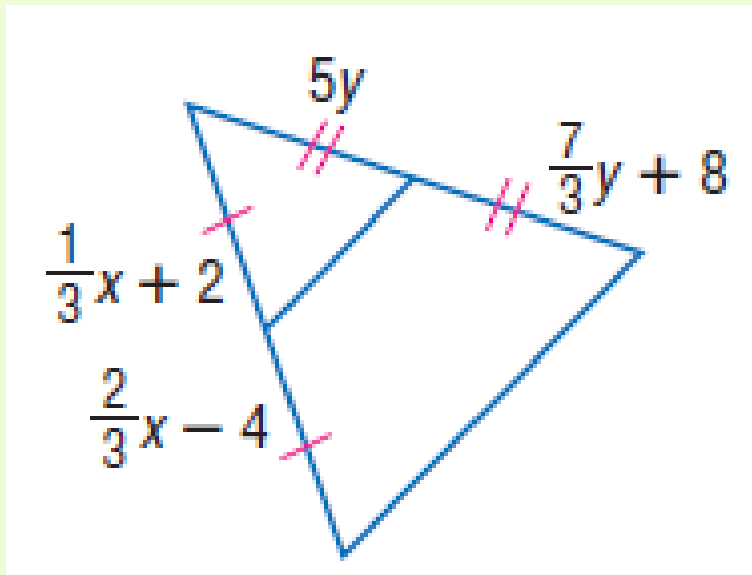
$$y = 5$$





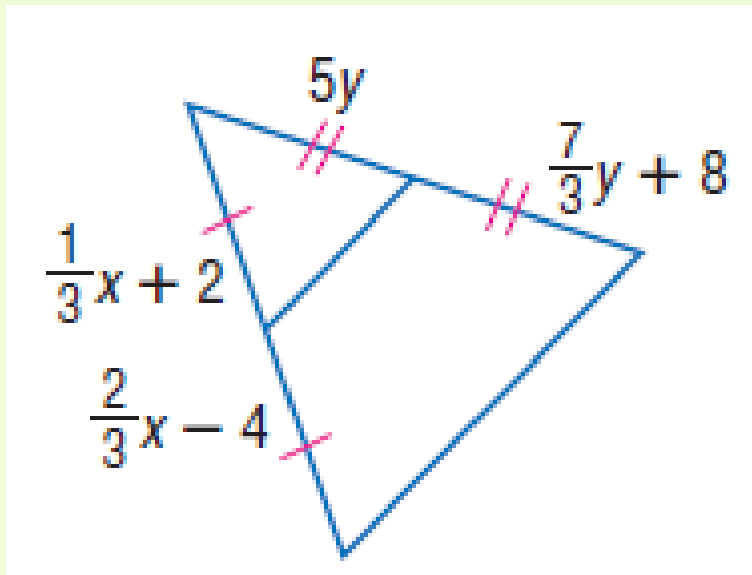
Examples

- Find x and y .



Examples

Find x and y .



Since the segments are congruent, simply set them equal to each other.

$$\frac{1}{3}x + 2 = \frac{2}{3}x - 4$$

$$5y = \frac{7}{3}y + 8$$

$$6 = \frac{1}{3}x$$

$$\frac{8}{3}y = 8$$

$$18 = x$$

$$y = 3$$

