

LESSON **Practice A**
8-8 Solving Radical Equations and Inequalities

Rewrite each equation to isolate the radical. The first one is done for you.

$$\begin{aligned} 1. \sqrt{x} - 6 &= 0 \\ + 6 & \quad + 6 \\ \hline \sqrt{x} &= 6 \end{aligned}$$

$$2. 8 + \sqrt{3x} - x = 0$$

$$3. \sqrt{2x+1} - 17 = 3x$$

Identify to what power each equation must be raised in order to solve. Then solve. The first one is done for you.

$$4. \sqrt[2]{x} = 4$$

$$5. \sqrt[4]{3x} = 12$$

$$6. \sqrt[3]{x+1} = 4$$

$$2; (\sqrt[2]{x^2}) = 4^2 = 16$$

Solve each equation or inequality. Then identify any extraneous solutions. The first one is done for you.

$$7. 2\sqrt{x+2} = 4$$

$$8. \sqrt{x+3} = x-3$$

$$\frac{2\sqrt{x+2}}{2} = \frac{4}{2}$$

$$\sqrt{x+2} = 2$$

$$(\sqrt{x+2})^2 = 2^2$$

$$x+2 = 4$$

$$x = 2, \text{ no extraneous roots}$$

Solve each equation or inequality.

$$9. \sqrt{x+2} = 5$$

$$10. (x+1)^{\frac{1}{3}} = 3$$

$$11. \sqrt{2x} - 6 < 0$$

$$12. \sqrt{3x+1} \geq 8$$

Solve.

13. Ainsley and Ben each solve the inequality $\sqrt{x+3} + 5 \leq 10$. Ainsley's solution is $x \leq 22$. Ben's solution is $-3 \leq x \leq 22$. Why are their solutions different? Which is correct?

LESSON

8-8

Practice A**Solving Radical Equations and Inequalities**

Rewrite each equation to isolate the radical. The first one is done for you.

$$\begin{aligned} 1. \sqrt{x} - 6 &= 0 \\ + 6 & \quad + 6 \\ \hline \sqrt{x} &= 6 \end{aligned}$$

$$2. 8 + \sqrt{3x} - x = 0$$

$$\sqrt{3x} = x - 8$$

$$3. \sqrt{2x+1} - 17 = 3x$$

$$\sqrt{2x+1} = 3x + 17$$

Identify to what power each equation must be raised in order to solve. Then solve. The first one is done for you.

$$4. \sqrt[2]{x} = 4$$

$$2; (\sqrt[2]{x^2}) = 4^2 = 16$$

$$5. \sqrt[4]{3x} = 12$$

$$4; x = \frac{69}{2}$$

$$6. \sqrt[3]{x+1} = 4$$

$$3; x = 63$$

Solve each equation or inequality. Then identify any extraneous solutions. The first one is done for you.

$$7. 2\sqrt{x+2} = 4$$

$$\frac{2\sqrt{x+2}}{2} = \frac{4}{2}$$

$$\sqrt{x+2} = 2$$

$$(\sqrt{x+2})^2 = 2^2$$

$$x+2 = 4$$

$$x = 2, \text{ no extraneous roots}$$

$$8. \sqrt{x+3} = x-3$$

$$x = 1, x = 6; x = 1 \text{ is an extraneous solution.}$$

Solve each equation or inequality.

$$9. \sqrt{x+2} = 5$$

$$x = 23$$

$$10. (x+1)^{\frac{1}{3}} = 3$$

$$x = 26$$

$$11. \sqrt{2x} - 6 < 0$$

$$0 \leq x < 18$$

$$12. \sqrt{3x+1} \geq 8$$

$$x \geq 21$$

Solve.

13. Ainsley and Ben each solve the inequality $\sqrt{x+3} + 5 \leq 10$. Ainsley's solution is $x \leq 22$. Ben's solution is $-3 \leq x \leq 22$. Why are their solutions different? Which is correct?

Ben's solution is correct. Ainsley forgot that the radicand cannot be negative.