Namo	Date	Class
	Duic	01000

## **Challenge 8-5** A Rational Method

Rational inequalities can be tricky to solve algebraically since it is often necessary to examine various possibilities.

Solve the inequality  $\frac{8}{x+5} \le 4$  algebraically.  $\frac{8}{x+5} - 4 \le 0$   $\frac{8}{x+5} - \frac{4(x+5)}{x+5} \le 0$   $\frac{-4x - 12}{x+5} \le 0$   $\frac{-4(x+3)}{x+5} \le 0$ 

This last inequality is true if the expression on the left of the inequality sign is equal to either 0 or a negative number. For the expression to be equal to 0, the numerator must be 0 and this occurs only at x = -3. For it to be negative, the numerator and denominator must have opposite signs. The table below lists the signs for the numerator and denominator in the intervals where neither numerator nor denominator is zero.

Interval	x < -5	-5 < x < -3	x > -3
Numerator	+	+	
Denominator	—	+	+
Rational Expression	_	+	_

For the inequality to be true, x < -5 or  $x \ge -3$ .

## Solve each inequality algebraically.

1. 
$$\frac{x+1}{x+3} < 2$$
  
2.  $\frac{x+4}{2x-1} \le 3$   
3.  $\frac{3}{x+3} > \frac{3}{x-2}$   
4.  $\frac{1}{x+1} > \frac{2}{x-1}$   
5.  $\frac{x^2-3x+2}{x^2-2x-3} \ge 0$   
6.  $\frac{x^2-4}{x^2-x-2} < 1$   
7.  $\frac{5-x}{x^2-25} \ge 1$   
8.  $\frac{3x}{x-5} < \frac{2}{8x-1}$   
9.  $\frac{5x}{x-2} < 7$ 

