## **Problem Solving 5-7** Solving Quadratic Inequalities

The manager at Travel Tours is planning a fall tour to Australia. He works out the details and finds that the profit *P* for *x* persons is  $P(x) = -28x^2 + 1400x - 3496$ . The owner of Travel Tours has decided that the tour will be canceled if the profit is less than \$10,000.

1. a. Write an inequality that you could use to find the number of people needed to make the tour possible.

$$-28x^{2} + 1400x - 3496 >$$

**b.** Solve the related equation to find the critical values.

## Solution:

Profit must be greater than 10,000.

$$-28x^2 + 1400x - 3496 \ge 10,000$$

 $-28x^2 + 1400x - 3496 = 10,000$ 

 $-28x^2 + 1400x - 13496 = 0$ 

Use quadratic formula.

x = 13.04, 36.96

**c.** Test an *x*-value in each interval.

<i>x</i> -value	Evaluate	<i>P</i> ≥ 10,000?
10	$-28(10)^2 + 1400(10) - 3496$	
30		
40		

**d.** How many people will Travel Tours need to make the tour possible?

The manager plans a tour to the Fiji Islands and determines that the profit *P* for *x* persons is  $P(x) = -40x^2 + 1920x - 3200$ . Choose the letter for the best answer.

- **3.** In order to make \$10,000 profit, how many people will it take for this tour to happen?
  - A Between 9 and 39 people
  - B Between 14 and 36 people
  - C At least 22 people

- **4.** The owner thinks the company should make at least \$15,000 profit on the Fiji Islands tour. How many people will it take for the tour to happen?
  - A Between 9 and 39 people
  - B Between 13 and 35 people
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Use quadratic formula.

*x* = 13.04, 36.96

**c.** Test an *x*-value in each interval.

<i>x</i> -value	Evaluate	<i>P</i> ≥ 10,000?
10	$-28(10)^2 + 1400(10) - 3496$	no
30	13,304	yes
40	7704	no

**d.** How many people will Travel Tours need to make the tour possible?

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From 14 to 36 people

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 $-28x^2 + 1400x - 3496 > 10,000$ 

*x* = 13.04, 36.96