Name	Date	Class

Challenge 4-4 Determinant Variations with Matrix Operations

What happens to the determinant of a matrix as the entries in the matrix are changed? Certain changes affect the value of the determinant and others do not. Those operations that do not change the determinant are called invariant operations. The determinant of matrix R is -36. Interchange the first and second rows to get matrix S.

			4		-3	2	5]	
R =	-3	2	5	S =				
	0	2	-1		0	2	-1	

1. a. Calculate the determinant of matrix S.

- **b.** Interchange the second and third rows of matrix *R*. Find the determinant of the new matrix. How do they compare?
- **c.** Make a conjecture about how the value of a matrix changes if you interchange two rows of the matrix.
- **2. a.** Multiply the first row of matrix *R* by 3. Now find the new determinant. How does this value compare to the original determinant?
 - **b.** Try this with another 3×3 matrix. Then make a conjecture about how the determinant changes when a row is multiplied by a constant.
- **3. a.** Multiply matrix *R* by 3 to get matrix *T*. Find the determinant of matrix *T*.
 - **b.** Now create a 2×2 matrix and find its determinant. Multiply the matrix by 4 and find the determinant again. Write a conjecture about how the determinant of a matrix changes when the matrix is multiplied by a constant.

- **4. a.** Use matrix *R* and add twice the first row to the second row. This becomes the new second row. Write the new matrix *U*. Find its determinant.
 - **b.** Try this with another 3 \times 3 matrix. What conjecture can you make about how this operation affects the determinant?

