

Study Guide and Intervention

Subtracting Functions Using Tables and Equations

Example Use a table to write a function rule for $h(x)$ if $f(x) = 3x + 2$ and $g(x) = x^2 - x$, and $h(x) = f(x) - g(x)$.

Solution

Step 1 Calculate the finite differences for the table

		1	1	1	1
x	-1	0	1	2	3
$f(x) = 3x + 2$	-1	2	5	8	11
$g(x) = x^2 - x$	2	0	0	2	6
$h(x) = f(x) - g(x)$	-3	2	5	6	5
		5	3	1	-1
			-2	-2	-2

Step 2 Use patterns in the finite differences to write a function rule for $n(x)$.

Since the second finite difference is constant, this is a quadratic function.

Input the values into the calculator and perform a quadratic regression.

Step 3: Write the values into the equation.

$$h(x) = -x^2 + 4x + 2$$

Exercises

For questions 1-4, use a table to write a function rule for $h(x)$.

1.

x	$f(x) = 3x + 7$	$g(x) = 8x - 3$	$h(x) = f(x) - g(x)$
1	10	5	5
2	13	13	0
3	16	21	-5
4	19	29	-10
5	22	37	-15
6	25	45	-20

2.

x	$f(x) = 4x^2 - 6$	$g(x) = -2x + 12$	$h(x) = f(x) - g(x)$
-3	30	18	12
-2	10	16	-6
-1	-2	14	-16
0	-6	12	-18
1	-2	10	-12
2	10	8	2

3.

x	$f(x) = 0.5x^2 - 3$	$g(x) = -x + 5$	$h(x) = f(x) - g(x)$
0	-3	5	-8
1	-2.5	4	-6.5
2	-1	3	-4
3	1.5	2	-0.5
4	5	1	4
5	9.5	0	9.5

4.

x	$f(x) = 2x^3 - 4x$	$g(x) = -2x + 12$	$h(x) = f(x) - g(x)$
-2	-8	16	-24
-1	2	14	-12
0	0	12	-12
1	-2	10	-12
2	8	8	0
3	42	6	36
4	112	4	108

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Subtracting Functions Using Tables and Equations (cont.)

Example If $h(x) = f(x) - g(x)$, $f(x) = -3(x + 1)^2 + 2$, and $g(x) = (x - 3)^2 - 4$, write the most simplified form of $h(x)$.

Solution

Step 1 Substitute the equations for $f(x)$ and $g(x)$ into the equation $h(x) = f(x) - g(x)$.

$$h(x) = f(x) - g(x)$$

$$h(x) = [-3(x + 1)^2 + 2] - [(x - 3)^2 - 4]$$

Step 2 Simplify the polynomial expression.

$$h(x) = [-3(x + 1)^2 + 2] - [(x - 3)^2 - 4]$$

$$h(x) = [-3(x + 1)(x + 1) + 2] - [(x - 3)(x - 3) - 4]$$

$$h(x) = [-3(x^2 + 2x + 1) + 2] - [x^2 - 6x + 9 - 4]$$

$$h(x) = [-3x^2 - 6x - 3 + 2] - [x^2 - 6x + 9 - 4]$$

$$h(x) = [-3x^2 - 6x - 1] - [x^2 - 6x + 5]$$

$$h(x) = -3x^2 - 6x - 1 - x^2 + 6x - 5$$

$$h(x) = (-3x^2 - x^2) + (-6x + 6x) + (-1 - 5)$$

$$h(x) = -4x^2 + 0x - 6$$

$$h(x) = -4x^2 - 6$$

Exercises

For problems 5 – 10, write the simplified form of $h(x)$ if $h(x) = f(x) - g(x)$.

5. $f(x) = 0.5x + 15$
 $g(x) = -3x - 5$

6. $f(x) = 2x^2 + 7$
 $g(x) = x^2 + 2x - 1$

7. $f(x) = x^3 - 2x$
 $g(x) = x^2 + 5$

8. $f(x) = 8x + 13$
 $g(x) = (x - 5)^2$

9. $f(x) = x^3 + 1$
 $g(x) = 5x + 9$

10. $f(x) = 5x - 3$
 $g(x) = 0.5x^2 - 4$