

## **Linear Functions**

- For a linear function, the general form is f(x) = a(bx c) + d, where a, b, c, and d are real numbers.
- The linear parent function is f(x) = x
- The full family of linear functions is generated by applying transformations to the linear parent function
- Transformations are applied using parameters that are multiplied or added to the independent variable in the functional relationship

### Changes in a

- The parameter *a* influences the vertical stretch or compression of the graph of the line.
- If |a| > 1, then the y-values are multiplied by a factor of *a* to vertically stretch the graph
- If o < |a| < 1, then the y-values are multiplied by a factor of a to vertically compress the graph









# Changes in b

- The parameter *b* influences the horizontal stretch or compression of the graph of the line.
- If |b| > 1, then the x-values are multiplied by a factor of 1|b| to horizontally compress the graph
- If o < |b| < 1, then the x-values are multiplied by a factor of  $\frac{1}{|b|}$  to horizontally stretch the graph





















		x	f(x) = x	x	f(x) = (x-5)
		-4	-4	1	-4
	Changes in c	-2	-2	3	-2
	X-values are increased by 5 in order to generate the same y-value. This addition results in a horizontal translation of the graph to the right.	0	0	5	0
		2	2	7	2
		4	4	9	4
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		x	f(x) = x	x	f(x) = (x+4)
		-4	-4	-8	-4
	Changes in c	-2	-2	-6	-2
	X-values are decreased by 4 in order to generate the same y-value. This subtraction results in a horizontal translation of the graph to the left.	0	0	-4	0
		2	2	-2	2
		4	4	0	4











• If the equation of the line is in the general form, y = a(bx - c) + d then:

- the x-intercept becomes  $(\frac{ac}{ab}, o)$
- the y-intercept becomes (o, -ac + d)

## Set Builder Notation

• The domain of a linear function is all real numbers. Using set builder notation the domain of a linear function is written as  $\{x \mid x \in \mathbb{R}\}$ 

• The range of a linear function is all real numbers. Using set builder notation the domain of a linear function is written as  $\{f(x) \mid f(x) \in \mathbb{R}\}$ 





#### Examples

- Step 2: Use the values of the parameters to describe the transformations of the linear parent function f(x) that are necessary to produce g(x).
- a = -3; so |a| > 1, then the y-values are multiplied by a factor of -3 to vertically stretch the graph and because a is negative, the graph is reflected over the x-axis
- b = 0.5; so 0 < |b| < 1, then the x-values are multiplied by a factor of  $\frac{1}{|0.5|} = 2$  to horizontally stretch the graph
- c = -4, so c < 0, then the graph will translate  $\left|\frac{-4}{0.5}\right| = 8$  to the left
- $d = \frac{2}{5}$ , so d > 0, then the graph of the line will translate  $\left|\frac{2}{5}\right|$  units up















