Study Guide and Intervention

Transforming and Analyzing Linear Functions

Example

Describe the transformation.

What transformations of the linear parent function, f(x) = x, will result in the graph of the linear function $g(x) = -3(0.5x + 4) + \frac{2}{5}$?

Solution

Step 1 Rewrite the equation of g(x) in general form to determine the values of the parameters a, b, c, and d.

$$g(x) = -3(0.5x + 4) + \frac{2}{5}$$

$$g(x) = -3(0.5x - \frac{(-4)}{5}) + \frac{2}{5}$$
Therefore, $a = -3$, $b = 0.5$, $c = -4$, and $d = \frac{2}{5}$,

Step 2 Use the values of the parameters to describe the transformations of the linear parent function f(x) that are necessary to produce g(x).

a = -3, so |a| >1. The range values (y-coordinates) of the linear parent function are multiplied by a factor of 3 in order to vertically stretch the graph. Since a is negative, the graph is also reflected over the x-axis.

b = 0.5, so 0 < b < 1. The domain values (x-coordinates) of the linear parent function are multiplied by a factor of $\frac{1}{0.5} = \frac{2}{100}$ in order to horizontally stretch the graph of the line.

c = -4, so c < 0. The graph of the linear parent function will translate $\left| \frac{-4}{0.5} \right| = 8$ units to the left

 $d = \frac{2}{5}$, so d > 0. The graph of the linear parent function will translate $\left|\frac{2}{5}\right| = \frac{2}{5}$ of a unit up.

Exercises

For questions 1-4, describe the transformation of the linear parent function, f(x) = x that will result in the graph of the linear function given.

1.
$$h(x) = (4x - 1)$$

2.
$$h(x) = 3(x+2)$$

3.
$$h(x) = -\frac{3}{4}(x-8) + 2$$

4.
$$h(x) = -4(\frac{1}{2}x - 3) + 4$$

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Transforming and Analyzing Linear Functions (cont.)

Identify the domain, range, x-intercept and y-intercept of the linear function described by the equation shown below. Write the domain and range as inequalities, as intervals, and in set builder notation.

$$f(x) = 4(x - 8) + 7$$

Solution

Determine the domain and range of f(x). Step 1

> Since this is a linear function, the domain and range are both all real numbers. As an inequality, this is written as

Domain:
$$-\infty < x < \infty$$
, Range: $-\infty < y < \infty$

As an interval

Domain:
$$(-\infty, \infty)$$
 Range: $(-\infty, \infty)$

Set builder notation

Domain: $\{x | x \in \mathbb{R}\}$ Range: $\{y | y \in \mathbb{R}\}$

Step 2 Determine the x-intercept of f(x).

x-intercepts occur where f(x) = 0

$$0 = 4(x - 8) + 7$$

$$0 = 4x - 32 + 7$$

$$0 = 4x - 25$$

$$0 + 25 = 4x - 25 + 25$$

$$25 = 4x$$

$$\frac{25}{4} = \frac{4x}{4}$$

$$6.25 = x$$

The x-intercept of f(x) is (6.25, 0)

Step 3 Determine the y-intercept of f(x).

y-intercepts occur where x = 0

$$\begin{split} f(0) &= 4(0-8) + 7 \\ f(0) &= 4(-8) + 7 \\ f(0) &= -32 + 7 \\ f(0) &= -25 \end{split}$$
 The y-intercept of f(x) is (0, -25)

Exercises

For questions 5-10, identify the domain, range, x-intercept and y-intercept of the linear function described by the equation shown below. Write the domain and range as inequalities, as intervals, and in set builder notation.

5.
$$f(x) = (2x + 3)$$

6.
$$f(x) = 4(\frac{1}{8}x + 2) - 5$$
 7. $f(x) = \frac{1}{4}(x + 8)$

7.
$$f(x) = \frac{1}{4}(x + 8)$$

8.
$$f(x) = -2(\frac{-1}{2}x + 3) + 5$$

9.
$$f(x) = \frac{-2}{5}(x + 8)$$

10.
$$f(x) = -3(2x + 5) + 9$$