

## Writing Linear Equations

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## Linear Function

- A linear function can be described by a linear equation.
- You can use function notation to show that the output value of the function  $f$ , written  $f(x)$ , corresponds to the input value  $x$ .

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## Linear Function

- Linear functions are functions with a constant rate of change and can be written in the form  $f(x) = mx + b$  where  $x$  is the independent variable and  $m$  and  $b$  are constants.
- The graph of a linear function is a straight line made up of the set of all points that satisfy  $y = f(x)$ .

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## Slope-Intercept Form

- An equation written in the form  $y = mx + b$

KEY CONCEPT		Slope-Intercept Form of a Linear Equation
<b>Words</b>	The slope-intercept form of the equation of a line is $y = mx + b$ , where $m$ is the slope and $b$ is the y-intercept.	
<b>Symbols</b>	$y = mx + b$ slope $\rightarrow$ $m$ $b$ $\rightarrow$ y-intercept	

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## Examples

- Write an equation in slope-intercept form for the line that has a slope of  $\frac{3}{2}$  and passes through  $(-4, 1)$

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## Examples

- Write an equation in slope-intercept form for the line that has a slope of  $\frac{3}{2}$  and passes through  $(-4, 1)$
- $y = mx + b$
- $1 = \frac{3}{2}(-4) + b$
- $1 = 6 + b$
- $-5 = b$
- $y = \frac{3}{2}x - 5$

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## Examples

- Write an equation in slope-intercept form for the line that has a slope of  $\frac{4}{3}$  and passes through (3, 2)

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## Examples

- Write an equation in slope-intercept form for the line that has a slope of  $\frac{4}{3}$  and passes through (3, 2)
- $y = mx + b$
- $2 = \frac{4}{3}(3) + b$
- $2 = 4 + b$
- $-2 = b$
- $y = \frac{4}{3}x - 2$

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## Examples

- Write an equation in slope-intercept form for the line that has a slope of -4 and passes through (-2, -2)

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### Examples

- Write an equation in slope-intercept form for the line that has a slope of -4 and passes through (-2, -2)
- $y = mx + b$
- $-2 = -4(-2) + b$
- $-2 = 8 + b$
- $-10 = b$
- $y = -4x - 10$

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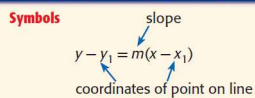
### Point-Slope Form

- An equation written in the form  $y - y_1 = m(x - x_1)$

**KEY CONCEPT**

*Point-Slope Form of a Linear Equation*

**Words** The point-slope form of the equation of a line is  $y - y_1 = m(x - x_1)$ , where  $(x_1, y_1)$  are the coordinates of a point on the line and  $m$  is the slope of the line.




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### Examples

- Write an equation in slope-intercept form for the line that passes through (2, 3) and (-4, -5)

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### Examples

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- Write an equation in slope-intercept form for the line that passes through (2, 3) and (-4, -5)

<ul style="list-style-type: none"> <li><math>m = \frac{y_2 - y_1}{x_2 - x_1}</math></li> <li><math>m = \frac{-5 - 3}{-4 - 2} = \frac{-8}{-6} = \frac{4}{3}</math></li> <li><math>y - y_1 = m(x - x_1)</math></li> <li><math>y - 3 = \frac{4}{3}(x - 2)</math></li> <li><math>y - 3 = \frac{4}{3}x - \frac{8}{3}</math></li> </ul>	<ul style="list-style-type: none"> <li><math>y = \frac{4}{3}x - \frac{8}{3} + 3</math></li> <li><math>y = \frac{4}{3}x - \frac{8}{3} + \frac{9}{3}</math></li> <li><math>y = \frac{4}{3}x + \frac{1}{3}</math></li> </ul>
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### Examples

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- Write an equation in slope-intercept form for the line that passes through (6, 1) and (8, -4)

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### Examples

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- Write an equation in slope-intercept form for the line that passes through (6, 1) and (8, -4)

<ul style="list-style-type: none"> <li><math>m = \frac{y_2 - y_1}{x_2 - x_1}</math></li> <li><math>m = \frac{-4 - 1}{8 - 6} = \frac{-5}{2}</math></li> <li><math>y - y_1 = m(x - x_1)</math></li> <li><math>y - 1 = \frac{-5}{2}(x - 6)</math></li> <li><math>y - 1 = \frac{-5}{2}x + \frac{30}{2}</math></li> </ul>	<ul style="list-style-type: none"> <li><math>y = \frac{-5}{2}x + 15 + 1</math></li> <li><math>y = \frac{-5}{2}x + 16</math></li> </ul>
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### Parallel and Perpendicular Lines

- We can use the slope-intercept and point-slope forms to write equations of lines that are parallel or perpendicular to other lines.

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### Parallel Lines

- Parallel lines are lines that lie in the same plane and do not intersect.
- Parallel lines have the same slope.

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### Examples

- Write an equation for the line that passes through  $(4, 6)$  and is parallel to the graph of  $y = \frac{2}{3}x + 5$ .

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### Examples

- Write an equation for the line that passes through (4, 6) and is parallel to the graph of  $y = \frac{2}{3}x + 5$ .

- $m = \frac{2}{3}$ ,  $P(4, 6)$        $y = \frac{2}{3}x - \frac{8}{3} + 6$
- $y - y_1 = m(x - x_1)$        $y = \frac{2}{3}x - \frac{8}{3} + \frac{18}{3}$
- $y - 6 = \frac{2}{3}(x - 4)$        $y = \frac{2}{3}x + \frac{10}{3}$
- $y - 6 = \frac{2}{3}x - \frac{8}{3}$

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### Perpendicular Lines

- Perpendicular lines are lines that lie in the same plane and intersect at right angles.
- Two lines are perpendicular if the product of their slopes is -1.
- Two lines are perpendicular if the slopes are negative reciprocals.

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### Examples

- Write the equation for the line that passes through (-3, -2) and is perpendicular to the graph of  $x + 4y = 12$ .

- Find the slope:  $\frac{1}{4}x$
- Find the negative reciprocal: -4
- Use point-slope form:  $y - y_1 = m(x - x_1)$
- $y + 2 = 4(x + 3)$
- $y = 4x + 12 - 2$
- $y = 4x + 10$

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