

EXPONENTIAL FUNCTIONS

- The exponential parent function is f(x) = b*.
 The full family of exponential functions is generated by applying transformations to the exponential parent function
- Transformations are applied using parameters that are multiplied or added to the independent variable in the functional relationship



- If $0 < |\, \alpha \,| < 1,$ then the y-values are multiplied by a factor of a to vertically compress the graph
- \bullet If a < 0, then the graph will be reflected across the x-axis

CHANGES IN K

- The parameter k influences the horizontal stretch or compression of the graph.
- If |k| > 1, then the x-values are multiplied by a factor of ¹/_{|k|} to horizontally compress the graph
- If $0 \le |k| \le 1,$ then the x-values are multiplied by a factor of $\frac{1}{|k|}$ to horizontally stretch the graph
- If k < 0, then the graph will be reflected across the y-axis

CHANGES IN C

• The parameter c, like k, influences the horizontal translation of the graph.

- Note that in the general form, the sign in front of the c is negative. This mean that when reading the value of c from the equation, you should read the opposite sign from what is given in the equation.
- If c > 0, then the graph will translate |^c/_v| to the right.
- If c < 0, then the graph will translate $|\frac{c}{k}|$ to the left.

CHANGES IN D

- The parameter d influences the vertical translation of the graph.
- If $d \ge 0$, then the graph of the parabola will translate |d| units up.
- If d < 0, then the graph of the parabola will translate |d| units down.

ASYMPTOTES

- Each exponential function has one horizontal asymptot
- The horizontal asymptote is governed by vertical parameters changes. A vertical translation moves the asymptote d units and a vertical dilation does not move the asymptote.

• horizontal asymptote: y = d

DOMAIN AND RANGE

- A exponential function does not have any domain restrictions. Therefore, the domain will always be all real numbers, or $\{x \mid x \in \mathbb{R}\}$
- The range is restricted by the horizontal asymptote, y = d. If a > 0, then the range is y > d. If a < 0, then the range is y < d.

• $a > 0, \{y \mid y > d\}$



• An exponential function has at most one x-intercepts. Use the graph and the calculator to determine the value of the x-intercept

• An exponential function has at most one y-intercepts. If it exists, the y-intercept is located at:

• $(0, \frac{a}{b^c} + d)$

EXAMPLES

• What transformations of the exponential parent function, $f(x) = 10^x$, will result in the graph of the exponential function $g(x) = -3(10)^{2x-1} + 5$?

EXAMPLES

 Step 1: Determine the values of the parameters a, k, c, and d of g(x) and the value of b, the base of g(x).

• a = -3, k = 2, c = 1, and d = 5

EXAMPLES

 Use the values of the parameters to describe the transformations of the exponential parent function f(x) that are necessary to produce g(x).

- c = 1: horizontal shift $\frac{1}{2}$ unit to the right
- d = 5; vertical shift 5 units up

EXAMPLES

• Identify the key attributes of $y = -2^{1.5x\cdot 3} + 1$, including domain and range, asymptote, x-intercept, and y-intercept. Write the domain and range in set builder notation.

EXAMPLES

Step 1: Determine the domain, range and asymptote of y = -2^{1.5x.3} + 1.
The domain is all real numbers; {x | x ∈ ℝ}
The range is affected by a and d; a is negative, d = 1
The range is numbers < 1; {y | y ≤ 1}



EXAMPLES

Step 2: Determine if the function has an x-intercept
The function has an x-intercept at (2, 0)

• Step 3: Determine if the function has a y-intercept

• The function has a y-intercept at (0, $\frac{7}{8}$)